# Considering Viscoelastic Micromechanics for the Reinforcement of Graphene Polymer Nanocomposites

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ABSTRACT: There has been much recent work investigating the reinforcement of glassy polymers with nanoparticles, and much excitement has been generated by some apparent synergies that suggest reinforcements greater than expected from elastic bound models. Here we show that it is necessary to consider the thermoviscoelastic response of the polymer matrix in nanocomposites (PNCs) to fully understand the reinforcement of the filler. This is especially so because polymer nanocomposites are frequently used at high fractions of the glass transition temperature  $T_{\rm g}$ , where the time dependence of the polymer is significant. Therefore it is a conceptual error to examine the modulus behavior of PNCs via only elastic micromechanics.



When the glass transition temperature increases due to the interactions between reinforcement and polymer, it is more reasonable to use a viscoelastic micromechanics approach to estimate the bounds on modulus behavior of PNCs. Here we use new results for grapheme oxide reinforced poly(ethyl methacrylate) (PEMA) and literature results for reinforced poly(methyl methacrylate) (PMMA) and show that the ultralow loading of graphene oxide raises the  $T_g$  of PEMA and PMMA significantly and leads to a large shift of the frequency−temperature properties of the polymer matrix. Our thermoviscoelastic approach shows that apparent extreme reinforcements can be attributed to the changing  $T_g$  of the polymer, and the corrected mechanical reinforcement from graphene oxide is much weaker than previously reported.

Recently, it has been reported<sup>1-3</sup> that dispersing graphene<br>or graphene oxide into polymer matrices at ultralow loadings (<0.50 vol %) can le[a](#page-3-0)d to excellent mechanical reinforcement of polymer nanocomposites (PNCs). In some instances, such as PMMA/graphene oxide (33% enhancement of Young's modulus E at only 0.005 vol  $\%)$ ,<sup>1</sup> results were interpreted to exceed the idealized Voigt upper bound prediction (the limit of infinite aspect ratio of fi[lle](#page-3-0)r and perfect alignment).5,9 The Halpin−Tsai model prediction<sup>7</sup> has also been exceeded in an epoxy/graphene system (31% increment of Young's [mo](#page-3-0)dulus at  $0.05$  vol  $\frac{6}{9}$ ).<sup>3</sup> The authors att[rib](#page-3-0)uted this high reinforcement to a hydrogen-bonding interaction<sup>1</sup> or an enhanced nanofiller-polymer mec[h](#page-3-0)anical interlocking due to the wrinkled morpholo[g](#page-3-0)y of graphene.<sup>1,3</sup> These striking results exceeding elastic micromechanics predictions lead to a great enthusiasm for the prospect of gr[aph](#page-3-0)ene polymer nanocomposites. At the same time, Kim et al. have questioned these surprising results and the associated explanations.<sup>6</sup>

An interesting phenomenon to be considered in what follows is that associated with the reported striking reinforcem[en](#page-3-0)t is a significant increase in the glass transition temperature  $(T_g)$ : 17 K at 0.005 vol % (PMMA/graphene oxide)<sup>1</sup> and 10 K at 0.05 vol % (epoxy/graphene).3,4 In Figure 1, constructed from Ruo[f](#page-3-0)f's data,<sup>2</sup> one can see that the increase of  $T_g$  and reinforcement for PMMA/graphe[ne](#page-3-0) oxide nanocomposites share a similar tren[d.](#page-3-0) This hint that  $T_g$  and modulus increases are correlated leads us to consider that the thermoviscoelasticity of the polymer matrix changes with the addition of the graphene or graphene oxide, and we propose that incorporation of viscoelastic



Figure 1. Glass transition temperature and storage tensile modulus E' of PMMA/graphene oxide at 313 K versus graphene oxide loading (data from ref 2).

micromechani[cs](#page-3-0) rather than conventional elastic micromechanics is necessary to describe the reinforcement of PNCs especially if the  $T_g$ of the matrix is changed by the addition of a nanofiller. As shown below, apparently high reinforcement can be attributed to the changing thermoviscoelasticity of the polymer matrix.

The most widely used elastic micromechanics theories are the Voigt upper bound mixing rule,<sup>5</sup> Halpin–Tsai equation,<sup>7</sup>



<span id="page-1-0"></span>and Mori−Tanaka model, $^8$  and they are used to predict elastic properties of composites.<sup>9,10</sup> To account for the polymer matrix viscoelasticity in comp[os](#page-3-0)ite materials, Hashin defined a viscoelastic micromecha[nics](#page-3-0) model for the modulus behav $ior^{11,12}$ 

$$
E_{\rm c}^{*}(i\omega) = V_{\rm m}E_{\rm m}^{*}(i\omega) + V_{\rm f}E_{\rm f}
$$
  

$$
E_{\rm m}^{*}(i\omega) = E_{\rm m}'(\omega) + iE_{\rm m}''(\omega)
$$
 (1)

where  $E^*$  is the complex modulus;  $V$  is the volume fraction of components; subscripts are m for the polymer matrix, f for filler, and c for composite.

In the present letter, we examine the influence of viscoelasticity of the polymer matrix on the PNCs reinforcement and especially consider changes in the viscoelastic properties induced by the changing  $T_g$  upon graphene oxide addition. We provide new experimental results for the glass transition and complex modulus of poly(ethyl methacrylate)/graphene oxide nanocomposites (PEMAGO) and consider literature data<sup>2</sup> for poly(methyl methacrylate)/graphene oxide nanocomposites (PMMAGO). A thermoviscoelastic micromechanics appr[o](#page-3-0)ach is presented to explain the reinforcement of graphene polymer nanocomposites.

Graphene oxide was exfoliated from graphite oxide (purchased from Graphene Laboratories, Inc.) by ultrasonication using a Misonix sonicator (XL 2000), then mixed with PEMA (purchased from Sigma-Aldrich,  $M_w = 515 \text{ kg/mol}$ ) using a solution-mixing procedure.<sup>1</sup> The graphene oxide was added to the system as 0.25 wt % or 0.12 vol %. Rectangular bar samples  $(1.3 \times 8.0 \times 45 \text{ mm}^3)$  and [cy](#page-3-0)lindrical samples (8.0 mm diameter, 1.1 mm height) were prepared through compression molding using a hot-press at 453 K. Dynamic mechanical properties were characterized using an ARES rheometer with a rectangular torsion fixture (from 230 to 330 K) and parallel plate fixture (from 330 to 370K). The glass transition temperature  $T_g$  was determined as the limiting fictive temperature<sup>13</sup>  $T_f^{\xi}$ , measured by a TA Q20 differential scanning calorimeter (DSC) by heating at 10 K/min after cooling at 10 K/min.

As seen in Table 1 and Figure 2, a significant increase in the glass transition temperature  $T_{\rm g}$  (nearly 15 K) was observed for

Table 1. Glass Transition Temperature of PEMA and PEMAGO

method	<b>PEMA</b>	$0.12$ vol % PEMAGO	$\Delta T_{\gamma}$
DSC.	337.4 K	352.2 K	14.8 K
rheometry (by the loss modulus $G''$ peak location in Figure 2)	334.6 K	350.8 K	16.2 K

the 0.12 vol % PEMAGO. This could be attributed to hydrogen bonding between graphene oxide and the carbonyl groups of PEMA, leading to a strong interaction of graphene oxide with the PEMA, as postulated for the PMMA/graphene system.<sup>1</sup> This is also similar to the increased  $T_{\rm g}$  values that have been reported in thin polymer films on substrates with strong inte[r](#page-3-0)actions,<sup>14</sup> such as PMMA on native silicon oxide.<sup>15</sup>

Figure 3 shows dynamic temperature ramp results for both the PE[MA](#page-3-0)GO from this work and the PMMAG[O](#page-3-0) from ref 2. The addi[tio](#page-2-0)n of graphene oxide causes a shift in the curves toward higher temperatures for both materials, consistent wi[th](#page-3-0) a nearly 15 K increment in  $T_g$  for the PEMAGO 0.12 vol %, 14 K for the PMMAGO 0.13 vol %, and 17 K for the PMMAGO



Figure 2. Loss modulus versus temperature for PEMA and PEMAGO 0.12 vol % from 320 to 370 K (heating rate at 1 K/min;  $\omega$  = 6.28 rad/s; strain is 0.02%).

1.0 vol %. Therefore, the polymer matrix with the graphene oxide seems to behave as the pure polymer at lower temperatures, showing the importance of the matrix thermoviscoelasticity. In addition, we can see for the PEMA peak of the loss shear modulus G", there is little change in the strength of the  $\beta$ relaxation, which means the graphene oxide does not reinforce the PEMA as an antiplastizer.<sup>16</sup>

Dynamic frequency sweep results for the PEMA and PEMAGO at different temp[era](#page-3-0)tures are shown in Figure 4. At 298 K (room temperature), the curves for G′ and G″ for the 0.12 vol % PEMAGO (solid square and solid diamond) overl[ap](#page-2-0) the curves of pure PEMA at 283 K (open circle and open triangle), which is consistent with the increase of 15 K in the  $T_g$ and for the frequency−temperature behavior of the polymer matrix.

To further explore the influence of the matrix thermoviscoelasticity and elasticity on the reinforcement for graphene polymer nanocomposites, the dynamic temperature ramp data were shifted to the same value of  $T - T_g$  in Figure 5. It is found that for the PEMA the curves for storage modulus G′ coincide well though the loss modulus curves do not overla[p](#page-2-0) well due to the  $\beta$  relaxation<sup>17</sup> (Figure 5a). In the case of the PMMA, it is found that  $E'$  and  $E''$  for the PMMAGO 0.13 vol % nearly overlap the PM[MA](#page-3-0) curves, [b](#page-2-0)ut the PMMAGO 1.0 vol % shows a slight vertical shift (Figure 5b).

The apparent experimental reinforcements can be obtained using eq 2 for the data of Fig[ur](#page-2-0)e 3. However, upon considering the thermoviscoelasticity, eq 2 was modified to eq 3 by replacing the modulus as function [of](#page-2-0) temperature by the modulus as function of  $T - T_{gt}$  to give corrected experimental reinforcements from the shifted data of Figure 5. In a similar manner the reinforcement prediction from the elastic Voigt upper bound (eq 4) was modified to the vi[sc](#page-2-0)oelastic Voigt upper bound (eq 5).

$$
\frac{E_{\rm c}(T)}{E_{\rm m}(T)} - 1\tag{2}
$$

$$
\frac{E_{\rm c}(T - T_{\rm g})}{E_{\rm m}(T - T_{\rm g})} - 1\tag{3}
$$

$$
\frac{V_{\rm m}E_{\rm m}(T) + V_{\rm f}E_{\rm f}}{E_{\rm m}(T)} - 1 \tag{4}
$$

<span id="page-2-0"></span>

Figure 3. Loss and storage moduli during temperature ramp for (a) PEMA and PEMAGO 0.12 vol % from 230 to 330 K (heating rate at 1 K/min;  $\omega$  = 6.28 rad/s; strain is 0.02%) and (b) PMMA and PMMAGO (data from ref 2).



Figure 4. Dynamic frequency sweep of PEMA and PEMAGO 0.12 vol % at 283 and 298 K (strain is 0.02%).

$$
\frac{V_{\rm m}E_{\rm m}(T - T_{\rm g}) + V_{\rm f}E_{\rm f}}{E_{\rm m}(T - T_{\rm g})} - 1
$$
\n(5)

It is worth noting that the interest in the Voigt bounds arises because properties that exceed these bounds are considered to be evidence for "extreme reinforcement" or synergistic reinforcement, which could be evidence for novel behavior in such nanocomposites.

The influence of viscoelasticity is more clearly illustrated in Figure 6, where the apparent experimental reinforcements (obtained by eq 2) are plotted for different temperatures and compared [to](#page-3-0) the elastic Voigt upper bound predictions (eq 4). The corrected r[ei](#page-1-0)nforcements obtained from eq 3 are also shown to compare with the viscoelastic Voigt upper bound [pre](#page-1-0)- dicti[on](#page-3-0)s (from eq 5) in Figure 6. Although the apparent uncorrected reinforcement is close to or even exceeds the elastic Voigt upper bound predi[cti](#page-3-0)on, it is clear that the corrected reinforcements are much weaker than the viscoelastic upper bound prediction.

Figure 6 demonstrates that in polymer nanocomposites, the apparent reinforcement can be attributed to the changed viscoelast[ic](#page-3-0)ity of the polymer induced by the  $T_{\sigma}$  change. The corrected effect of the graphene oxide reinforcement on PEMA and PMMA at ultralow loading is not as high as has been reported and accounting for the viscoelastic response indicates less reinforcement than estimated from the elastic bound, hence providing a reason to Kim et al.'s skepticism concerning claims of extreme reinforcement. It may also explain Ruoff's work with polycarbonate/graphene oxide that exhibits weak reinforcement, where little  $T_{\rm g}$  change is seen.<sup>18</sup>

The results presented here show that it is necessary to consider the thermoviscoelastic resp[ons](#page-3-0)e of the polymer matrix in nanocomposites (PNCs) to fully understand the reinforcement of the filler. This is especially so because polymer nanocomposites are frequently used at high fractions of the  $T_{\mathcal{Q}}$ , where the time dependence of the polymer is significant.<sup>19</sup> Therefore it is a conceptual error to examine the modulus behavior of PNCs via only elastic micromechanics. When t[he](#page-3-0) glass transition temperature increases, the polymer matrix in the PNCs behaves as the pure polymer at a lower temperature, contradicting the inherent assumption in elastic micromechanics. Consequently, it is more reasonable to use Hashin's viscoelastic micromechanics model, taking into account changes in matrix response due to the addition of the filler, to estimate



Figure 5. Storage modulus and loss modulus versus  $T - T_g$  of (a) PEMA and PEMAGO 0.12 vol % and (b) PMMA and PMMAGO (data from ref 2).

<span id="page-3-0"></span>

Figure 6. Apparent and corrected reinforcements and Voigt upper bound predictions for  $(a, b)$  PEMAGO 0.12 vol %  $(\omega = 6.28 \text{ rad/s})$  and  $(c, d)$ PMMAGO 0.13 vol %  $(f = 1Hz)$  (data from ref 2).

the bounds on modulus behavior of PNCs.<sup>11,12</sup> At temperatures much farther below  $T_g$  or when there is no change of  $T_g$ , the changes in the viscoelasticity of the polymer matrix are less important, and the elastic micromechanics might be considered to capture the approximate reinforcement behavior of PNCs.

In summary, we have demonstrated that the ultralow loading of graphene oxide raises the  $T_{\rm g}$  of PEMA and PMMA significantly and leads to a large shift of the frequency−temperature properties of the polymer matrix. In such a condition, it is necessary to consider the influence of thermoviscoelasticity on the expected reinforcement in graphene oxide polymer nanocomposites, and Hashin's viscoelastic micromechanics should be considered. Our thermoviscoelastic approach shows that apparent extreme reinforcements can be attributed to the changing  $T_g$  of the polymer, and the corrected mechanical reinforcement from graphene oxide is much weaker than previously reported.

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#### **Notes**

The auth[ors declare no competi](mailto:greg.mckenna@ttu.edu)ng financial interest.

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### ■ REFERENCES

(1) Ramanathan, T.; Abdala, A. A.; Stankovich, S.; Dikin, D. A.; Herrera-Alonso, M.; Piner, R. D.; Adamson, D. H.; Schniepp, H. C.;

Chen, X.; Ruoff, R. S.; Nguyen, S. T.; Aksay, I. A.; Prud'Homme, R. K.; Brinson, L. C. Nat. Nanotechnol. 2008, 3, 327−331.

- (2) Potts, J. R.; Lee, S. H.; Alam, T. M.; An, J.; Stoller, M. D.; Piner, R. D.; Ruoff, R. S. Carbon 2011, 49, 2615−2623.
- (3) Rafiee, M. A.; Rafiee, J.; Wang, Z.; Song, H.; Yu, Z.-Z.; Koratkar, N. ACS Nano 2009, 3, 3884−3890.
- (4) Yavari, F.; Rafiee, M. A.; Rafiee, J.; Yu, Z.-Z.; Koratkar, N. ACS Appl. Mater. Interfaces 2010, 2, 2738−2743.
- (5) Liu, B.; Feng, X.; Zhang, S. Compos. Sci. Technol. 2009, 69, 2198− 2204.
- (6) Kim, H.; Abdala, A. A.; Macosko, C. W. Macromolecules 2010, 43, 6515−6530.
- (7) Halpin, J. C. J. Compos. Mater. 1969, 3, 732−734.
- (8) Mori, T.; Tanaka, K. Acta Metall. 1973, 21, 571−574.
- (9) Fornes, T. D.; Paul, D. R. Polymer 2003, 44, 4993−5013.
- (10) Tucker, C. L.; Liang, E. Compos. Sci. Technol. 1999, 59, 655−671.
- (11) Hashin, Z. J. Appl. Mechanics 1965, 32, 630−636.
- (12) Hashin, Z. Int. J. Solids Struct. 1970, 6, 797−807.
- (13) Badrinarayanan, P.; Zheng, W.; Li, Q.; Simon, S. L. J. Non-Cryst. Solids 2007, 353, 2603−2612.
- (14) Alcoutlabi, M.; McKenna, G. B. J. Phys.: Condens. Matter 2005, 17, 461−524.

(15) Keddie, J. L.; Jones, R. A. L.; Cory, R. A. Faraday Discuss. 1994, 98, 219−230.

- (16) Robeson, L. M.; Faucher, J. A. Polym. Lett. 1969, 7, 35−40.
- (17) Kulik, A. S.; Beckham, H. W.; Schmidt-Rohr, K.; Radloff, D.; Pawelzik, U.; Boeffel, C.; Spiess, H. W. Macromolecules 1994, 27, 4746−4754.
- (18) Potts, J. R.; Murali, S.; Zhu, Y.; Zhao, X.; Ruoff, R. S. Macromolecules 2011, 44, 6488−6495.

(19) McKenna, G. B. Dynamics of materials at the nanoscale. In Polymer Physics: From suspensions to nanocomposites and beyond; Utracki, L. A., Jamieson, A. M., Eds.; Wiley: New York, 2010; Chapter 5, pp 191−223.